We introduce an infinite sequence of systems of nonlinear Diophantine equations of a particular form. We prove that the number of positive solutions to the arbitrary system is finite. We then define and study a sequence (OEIS A275234) based on the numbers of solutions to the systems.